

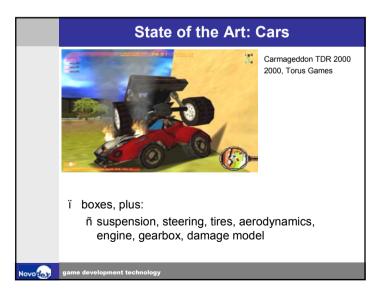
	Isnít Rigid Body Dynamics a solved problem? why classic robotics research is only a start:		
		Robotics	Games
	Problem size	~1 robot	virtual world
	Configuration	derive motion eqs for one robot	very dynamic
	Mechanisms	robot created so that motion eqs are simple	anything, ev. very redundant
	Constraints	primarily equality (joints)	primarily inequality (contacts)
	Accuracy	simulation	visually OK

Isnít Rigid Body Dynamics a solved problem?

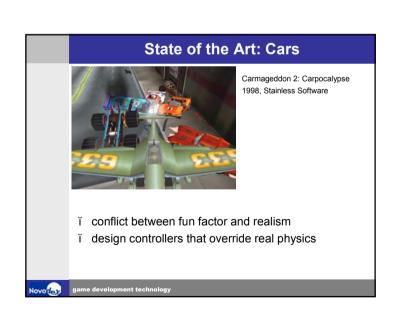
- ï a recent very relevant research paper:
- S. Redon, et al. Gauss' least constraints principle and rigid body simulations. may 2002.
- ï four game middleware companies use four conceptually very different simulation approaches
- ï I want to knock over a house made of individual bricks in real time...

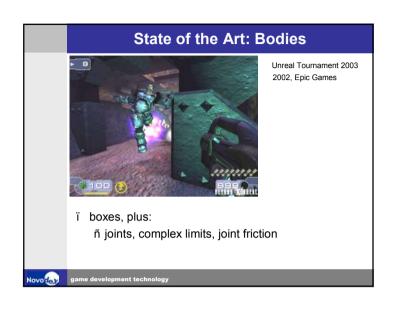
Novo de y

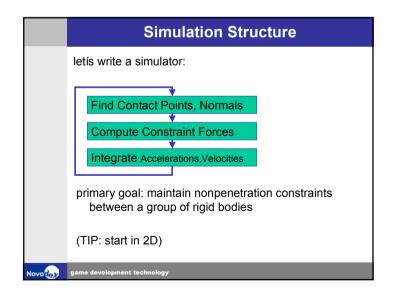
game development technology

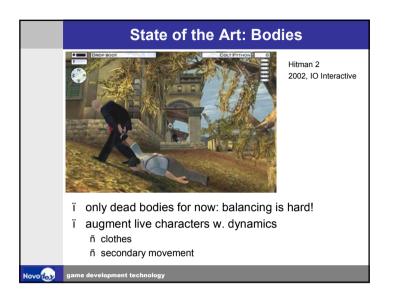


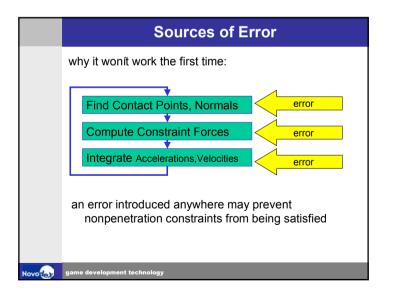
Trespasser 1998, Dreamworks interactive i universally applicable i stress test for technology: who can make the tallest stack? i good friction model is important

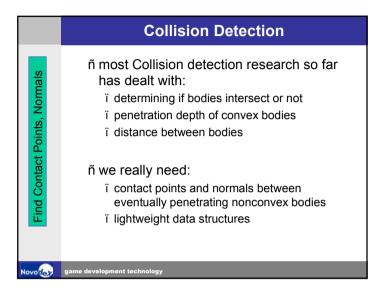


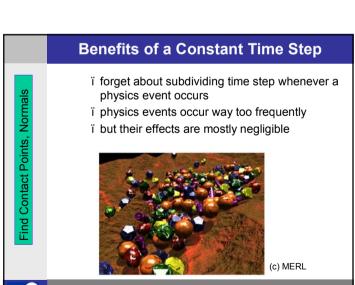


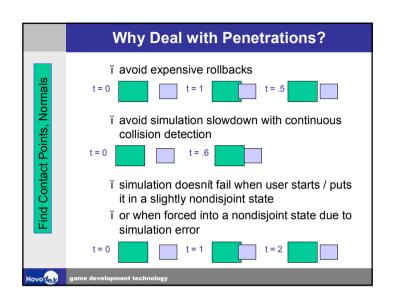


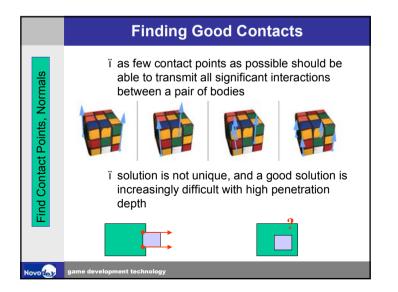




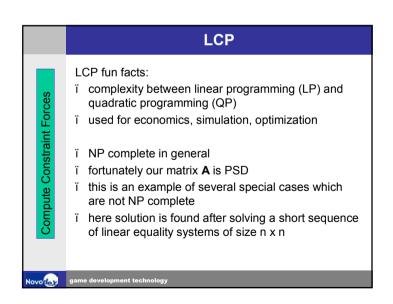


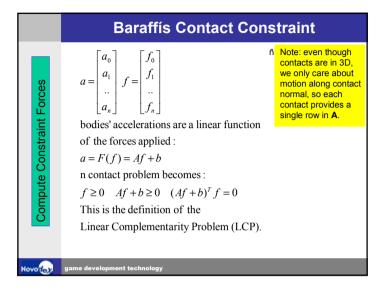


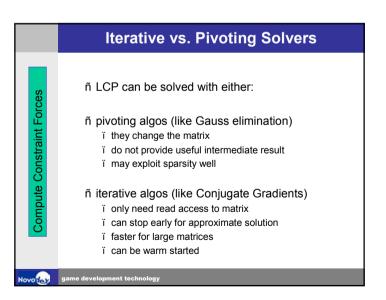




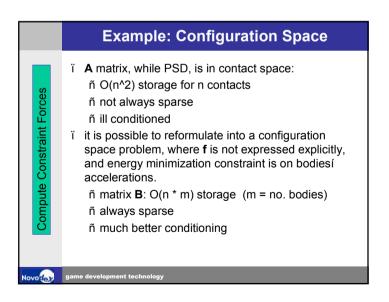
Baraffís Contact Constraint $a_i \ge 0$ nonpenetration constraint However, this does not uniquely determine the normal force. Additional constraints: $f_i \ge 0$ contact force is repulsive $f_i a_i = 0$ constraint force is workless $(\Leftrightarrow \text{if } (f_i) \text{then } a_i = 0; \text{ if } (a_i) \text{then } f_i = 0;)$ Stack n contacts' variables. Matrix form: $a = \begin{bmatrix} a_0 \\ a_1 \\ \vdots \\ a_n \end{bmatrix} f = \begin{bmatrix} f_0 \\ f_1 \\ \vdots \\ f_n \end{bmatrix}$



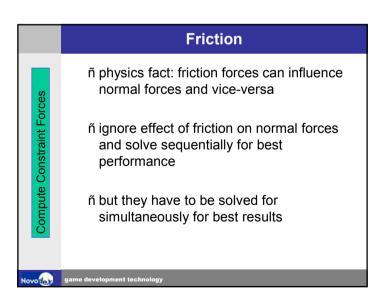




Equivalence to LCP ñ if you are computing contact forces to satisfy nonpenetration constraints in any way, you have written a certain kind of LCP solver ñ even if you are using simple penalty methods ñ because if any of below don't hold, you don't have realistic motion: ï **f** >= 0 a >= 0fa = 0ñ if your sim is only approximate, then the LCP solution is approximate ï for example penalty methods are usually &bouncyí ï (= the contacts are not quite workless) ï So |fa| < eps me development technology



To does this mean we can'tt write a better contact force solver than what is in the LCP textbooks? I matrix A does not have to be explicit n x n I a and f do not have to be stored explicitly either I you can work in a different space I you can approximate in a wide variety of ways I you can always come up with a transform of your inputs / outputs to a classic LCP formulation I if you introduce more complex constraints, for the sake of realism, you may end up with a QP or NCP problem; the LCP is a special case.



Joints

ñ the joint forces of an articulated system are equality constraints:

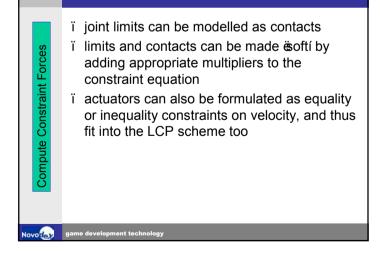
$$a_i = 0$$
$$a = Af + b = 0$$

ñ solve for **f** with any linear system solver ñ but special properties of A (PSD, symmetric, sparse, etc.) make a carefully chosen solver superior

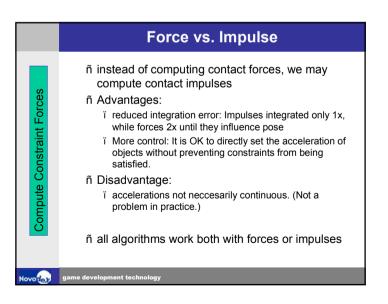


game development technology

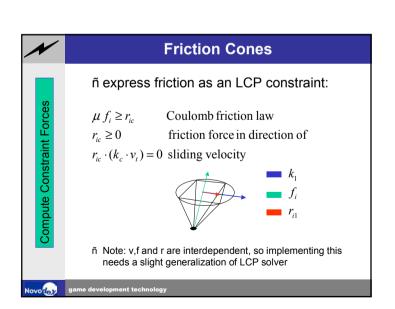
Joint Limits and Actuators



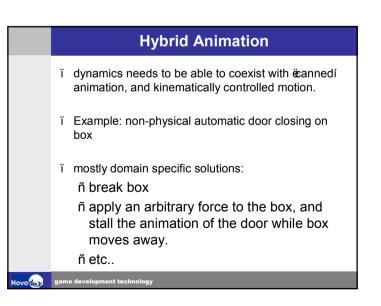
n an articulated system with contact constraints results in both equality and complementarity constraints to be solved for simultaneously n Mixed Linear Complementarity Problem n first m rows of A do not have constraint on corresp terms of f, and =0, instead of >0 n pivoting or iterative LCP solvers can be generalized to solve MLCPs



n classical way to cope with integration error is to choose higher order integrator nust integration and contact force determination be separate? if the algorithm computing the contact forces knows about they type of integration scheme used, it can anticipate its error, and compensate for it. if this way even fast Euler integration works great if Big disadvantage: external effects not formulated as constraints have severe integration error



Work at NovodeX i If you are already knew all this and are interested in an exciting job or internship, contact me: adam.moravanszky@novodex.com or Matthias M, Iler.



ntegration nthus two common scenarios: nthus two common s

