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## Raycasting

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### Direct volume rendering

Volume rendering (sometimes called **direct volume rendering**) stands for methods that generate images directly from 3D scalar data.

"Directly" means: **no intermediate geometry** (such as an isosurface) is generated.

Volume rendering techniques

- depend strongly on the grid type
- exist for structured and unstructured grids
- are predominantly applied to uniform grids (3D images).

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### Direct volume rendering

2D or 3D image data are uniform grids with **cell-centered data**.  
Cell-centered data

- are attributed to cells (pixels, voxels) rather than nodes
- can also occur in (finite volume) CFD datasets
- are converted to node data
  - by taking the **dual grid** (easy for uniform grids,  $n$  cells  $\rightarrow n-1$  cells!)
  - or by interpolating.

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### Raycasting

**Raycasting** is historically the first volume rendering technique.

It has common with **raytracing**:

- **image-space** method: main loop is over pixels of output image
  - a **view ray** per pixel (or per subpixel) is traced backward
  - samples are taken along the ray and **composited** to a single color
- Differences are:
- no secondary (reflected, shadow) rays
  - transmitted ray is not refracted
  - more elaborate compositing functions
  - samples are taken at intervals (not at object intersections)

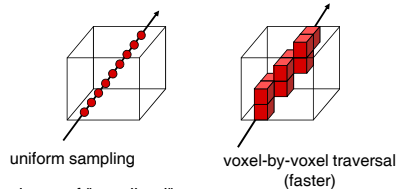
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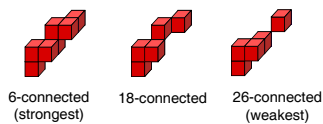
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### Raycasting

Sampling interval can be fixed or adjusted to voxels:



Connectedness of "voxelized" rays:



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### Ray templates

A **ray template** (Yagel 1991) is a voxelized ray which by translating generates all view rays.

Ray templates speed up the sampling process, but are obviously restricted to **orthographic** views.

Algorithm:

- Rename volume axes such that  $z$  is the one "most orthogonal" to the image plane.
- Create ray template with 3D version of **Bresenham** algorithm, giving 26-connected rays which are functional in  $z$  coordinate (have exactly one voxel per  $z$ -layer)
- Translate ray template in **base plane**, not in image plane

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*Ray templates*

Incorrect: translated in image plane

Correct: translated in base plane

← base plane →

image plane

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*Compositing*

Two simple compositing functions can be used for previewing:

- **Maximum intensity projection (MIP):**
  - maximum of sampled values
  - result resembles X-ray image
- **Local maximum intensity projection (LMIP):**
  - first local maximum which is above a prescribed threshold
  - approximates occlusion
  - faster & better(!)

intensity

LMIP MIP threshold 0

← camera

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*Compositing*

Comparison of techniques (Y. Sato, dataset of a left kidney):  
Isosurface vs. raycasting with MIP, LMIP,  $\alpha$ -compositing

fast (1 parameter)	fast parameter free	fast (1 parameter)	-
-	full data range	full data range	-
-	noise insensitive	noise insensitive	-
lighting	-	-	full data range
occlusion (transparency)	-	(occlusion)	noise insensitive
-	-	-	lighting
-	-	-	occlusion
-	-	-	transparency

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*$\alpha$ -compositing*

Assume that each sample on a view ray has **color** and **opacity**:

$$(C_0, \alpha_0), \dots, (C_N, \alpha_N) \quad C_i \in [0, 1]^3, \alpha_i \in [0, 1]$$

where the 0<sup>th</sup> sample is next to the camera  
and the N<sup>th</sup> one is a (fully opaque) background sample:

$$C_N = (r, g, b)_{\text{background}}$$

$$\alpha_N = 1$$

$\alpha$ -compositing can be defined recursively:

Let  $C_i^b$  denote the **composite color** of samples  $f, f+1, \dots, b$

Recursion formula for **back-to-front** compositing:

$$C_b^b = \alpha_b C_b$$

$$C_f^b = \alpha_f C_f + (1 - \alpha_f) C_{f+1}^b$$

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*$\alpha$ -compositing*

The first few generations, written with **transparency**  $T_i = 1 - \alpha_i$

$$C_b^b = \alpha_b C_b$$

$$C_{b-1}^b = \alpha_{b-1} C_{b-1} + \alpha_b C_b T_{b-1}$$

$$C_{b-2}^b = \alpha_{b-2} C_{b-2} + \alpha_{b-1} C_{b-1} T_{b-2} + \alpha_b C_b T_{b-1} T_{b-2}$$

$$C_{b-3}^b = \alpha_{b-3} C_{b-3} + \alpha_{b-2} C_{b-2} T_{b-3} + \alpha_{b-1} C_{b-1} T_{b-2} T_{b-3} + \alpha_b C_b T_{b-1} T_{b-2} T_{b-3}$$

reveal the **closed formula** for  $\alpha$ -compositing:

$$C_f^b = \sum_{i=f}^b \alpha_i C_i \prod_{j=f}^{i-1} T_j$$

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*$\alpha$ -compositing*

**front-to-back** compositing can be derived from the closed formula:

Let  $T_f^b$  denote the **composite transparency** of samples  $f, f+1, \dots, b$

$$T_f^b = \prod_{j=f}^b T_j$$

Then the **simultaneous recursion** for front-to-back compositing is:

$$C_f^f = \alpha_f C_f$$

$$T_f^f = 1 - \alpha_f$$

$$C_f^{b+1} = C_f^f + \alpha_{b+1} C_{b+1} T_f^b$$

$$T_f^{b+1} = (1 - \alpha_{b+1}) T_f^b$$

Advantage of front-to-back compositing: **early ray termination** when composite transparency falls below a threshold.

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### The emission-absorption model

How realistic is  $\alpha$ -compositing?

The **emission-absorption** model (Sabella 1988) yields a basic **volume rendering equation**

$$L(x) = \int_x^{x_b} \epsilon(x') e^{-\int_x^{x'} \tau(x'') dx''} dx'$$

The equation describes the **radiance** (power per unit area per solid angle [W/m<sup>2</sup>/sr]) arriving along a ray at the position  $x$  on this ray.

The **emission** function  $\epsilon(x)$  describes the photons "emitted" by the volume along the ray.

The **absorption** function  $\tau(x)$  is the probability that a photon traveling over a unit distance is lost by absorption.

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### The emission-absorption model

The emission-absorption model is based on Boltzmann's transport equation in statistical physics, but completely ignores **scattering**.

In more general models  $\tau(x)$  is an **extinction function** having both an absorption term and a scattering term.

Instead, in the emission-absorption model:

- **incident scattering** is modeled by the emission function
- **loss by scattering** can be thought to be part of the absorption.

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### The emission-absorption model

Discrete version of emission-absorption model

$$L(x) = \sum_{i=0}^n \epsilon_i \Delta x e^{-\sum_{j=0}^{i-1} \tau_j \Delta x} = \sum_{i=0}^n \epsilon_i \Delta x \prod_{j=0}^{i-1} e^{-\tau_j \Delta x}$$

matches the  $\alpha$ -compositing formula

$$C_i^b = \sum_{i=f}^b \alpha_i C_i \prod_{j=f}^{i-1} (1 - \alpha_j)$$

and gives interpretations of "opacity" and "color":

$$\alpha_i = 1 - e^{-\tau_i \Delta x}$$

$$\alpha_i C_i = \epsilon_i \Delta x$$

The product  $\tilde{C}_i = \alpha_i C_i$  is called a **premultiplied** or **associated color**.

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### Transfer functions

**Transfer functions** map raw voxel data to opacities and colors as needed for the  $\alpha$ -compositing.

Inputs of TF (one or more):

- voxel value  $s(\mathbf{x})$
- gradient magnitude  $\|\nabla s(\mathbf{x})\|$
- higher derivatives of  $s(\mathbf{x})$

**Opacity transfer function**  $\alpha(s(\mathbf{x}), \|\nabla s(\mathbf{x})\|, \dots)$

**Color transfer function**  $C(s(\mathbf{x}), \|\nabla s(\mathbf{x})\|, \dots)$

– or premultiplied:  $\tilde{C}(s(\mathbf{x}), \|\nabla s(\mathbf{x})\|, \dots)$

In general TF don't depend on **spatial location**,  
exception: for **focus+context** techniques

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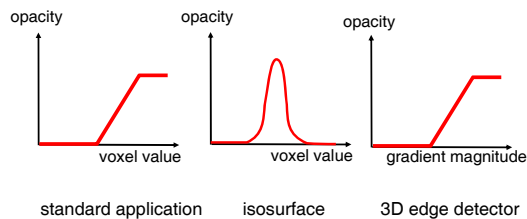
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### Transfer functions

By choosing different opacity transfer functions different types of applications can be achieved.

Examples:



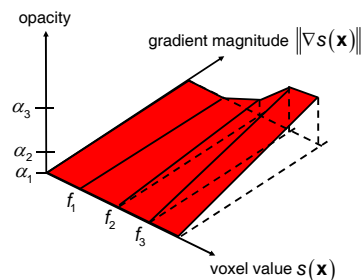
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### Transfer functions

Example of a **bivariate** (=2D) transfer function:



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*Transfer functions*

Example: bivariate transfer function for isosurface of constant "thickness".

opacity

gradient magnitude  $\|\nabla s(\mathbf{x})\|$

$f_0$

voxel value  $s(\mathbf{x})$

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*Transfer functions*

The color transfer function allows to make a simple **classification**.

Example:

color (RGB)

air fat tissue bone

voxel value  $s(\mathbf{x})$

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*Transfer functions*

Better (but more expensive) classification than with a transfer function is obtained by **segmentation** (typically slice by slice, semi-automatic).  
**Pre-classified** volume data.  
 Example: "virtual frog" dataset (Lawrence Berkeley Labs).

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*Transfer functions*

Volume rendering of segmented volume data (from VTK book).

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*Transfer functions*

Example: classifications with different transfer functions (McGill Univ.)

Example: temperature data for opacity and color TF (Nissan Res.Ctr.)

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*Transfer functions*

In pre-classification, the voxels can also be lit:

- The gradient is perpendicular to the local isosurface. It can be used as a normal vector for a **Phong lighting** (without rendering the isosurface itself).
- **Reflection coefficients** can be assigned by a separate transfer function ("materials" instead of colors only).
- The **diffuse lighting** can be applied to the entire volume dataset as a pre-processing since it is independent of the viewing direction.

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### Pre- vs. post-classification

For quality reasons, current volume rendering implementations often use **post-classification**.

#### Pre-Classification:

1. Transfer functions are applied to voxels
2. Results are interpolated to sample locations.

#### Post-Classification:

1. Raw data are interpolated to sample locations.
2. Transfer functions are applied to sampled data.

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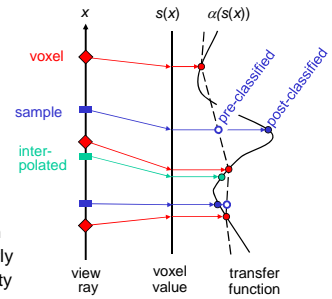
### Pre- vs. post-classification

Pre-classification:

- can be done as pre-processing, e.g. segmentation, diffuse lighting

Post-classification:

- Interpolation is in the correct space
- Additional samples can be interpolated on the fly to improve output quality

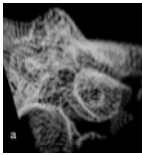


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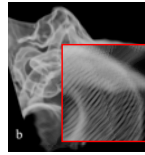
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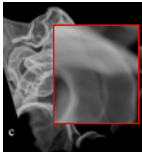
### Pre- vs. post-classification



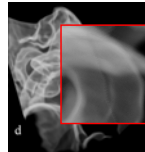
128 slices pre-classification



128 slices post-classification



284 slices post-classification



128 slices preintegrated

Image credit: K. Engel, U. Stuttgart

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### Preintegration

Idea (Engel 2001):

- simulate **infinitely many** interpolated samples between two successive samples  $s_i = s(\mathbf{x}_i)$  and  $s_{i+1} = s(\mathbf{x}_{i+1})$
- assuming:
  - field  $s(\mathbf{x})$  varies **linearly** between samples
  - transfer functions don't depend on derivatives

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### Preintegration

The discrete formula for opacity at a sample was

$$\alpha_i = 1 - e^{-\tau_i \Delta x}$$

The continuous version, for a sample interval  $[x_i, x_{i+1}]$ , is

$$\alpha_i = 1 - e^{-\int_{x_i}^{x_{i+1}} \tau(s(x)) dx}$$

Assuming now  $s(\mathbf{x})$  to be linear between samples, we get

$$\alpha_i = 1 - e^{-\frac{d}{s_{i+1} - s_i} \int_{s_i}^{s_{i+1}} \tau(s) ds} \quad \text{with } d = \|\mathbf{x}_{i+1} - \mathbf{x}_i\|$$

which is called a **preintegrated opacity transfer function**.

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### Preintegration

The integral

$$\int_{s_i}^{s_{i+1}} \tau(s) ds = \int_0^{s_{i+1}} \tau(s) ds - \int_0^{s_i} \tau(s) ds$$

can be evaluated by two lookups in a precomputed table of

$$\int_0^s \tau(s') ds'$$

Alternatively, the preintegrated opacity TF could be tabulated for **all possible combinations** of  $(s_i, s_{i+1}, d)$ , especially if the sampling distance  $d$  is chosen constant.

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Preintegration

The composite color of the same interval

$$C_i = \int_{x_j}^{x_{j+1}} \varepsilon(s(x)) e^{-\int_{x_j}^x \tau(s(x')) dx'} dx$$

simplifies for linear s(x) to

$$C_i = \frac{d}{s_{i+1} - s_i} \int_{s_i}^{s_{i+1}} \varepsilon(s) e^{-\frac{d}{s_{i+1} - s_i} \int_{s_i}^s \tau(s') ds'} ds$$

which is a **preintegrated color transfer function**.

Again, it can be tabulated for all combinations of  $(s_i, s_{i+1}, d)$ , or it can be approximately calculated from tabulated values of

$$\int_0^s \tau(s') ds' \text{ and } \int_0^s \varepsilon(s') ds' \text{ (moving the exponential term out of the integral).}$$

Raycasting hardware

Today's GPUs are well suited for volume rendering.

Object-space methods are more straight-forward, but also some raycasting implementations on GPUs have been done.

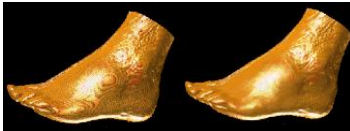
In contrast, two examples of special raycasting hardware:

- VIZARD (1997, U. Tübingen):
  - FPGA-based system
  - long pre-processing
  - 10 Hz for 256<sup>3</sup> volume
  - perspective view raycasting

Raycasting hardware

volumePRO (1999, MERL):

- PCI board
- no pre-processing
- 30 Hz for 256<sup>3</sup> volume
- orthographic raycasting
- ray templates
- shear-warp method
- z-supersampling



Example: with / without supersampling

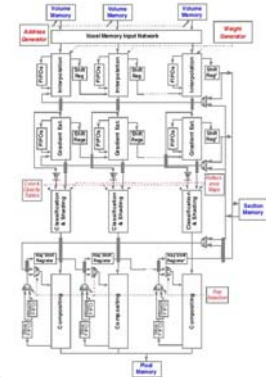
Raycasting hardware

ASIC chip of VolumePRO vg500 board has 4 parallel pipelines with stages:

- interpolation
- gradient estimation
- classification/shading
- compositing

Image is rendered in a single pass through the volume.

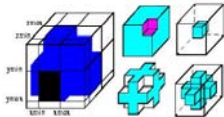
Off-chip memory for slices (shown in blue)



Raycasting hardware

Some special features:

- cropping
- clipping planes



some possible combinations of cropping and clipping planes

